



# Multi-scale structural similarity index for motion detection



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## KEYWORDS

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**Abstract** The most recent approach for measuring the image quality is the structural similarity index (SSI). This paper presents a novel algorithm based on the multi-scale structural similarity index for motion detection (MS-SSIM) in videos. The MS-SSIM approach is based on modeling of image luminance, contrast and structure at multiple scales. The MS-SSIM has resulted in much better performance than the single scale SSI approach but at the cost of relatively lower processing speed. The major advantages of the presented algorithm are both: the higher detection accuracy and the quasi real-time processing speed.

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## 1. Introduction

Fighting terrorism is becoming imperative and is driving researchers toward designing robust video surveillance systems. Event detection and analysis is one of the major applications of video surveillance. A first step in video event analysis is motion detection. A motion detection algorithm should avoid releasing false alarms by considering image luminance, contrast and structure at multiple scales. Accurate

motion detection algorithms are the key components of video surveillance systems. It can be applied as well in some interesting applications such as the automatic light control and automatic door opening in smart homes and work areas resulting in efficient energy use.

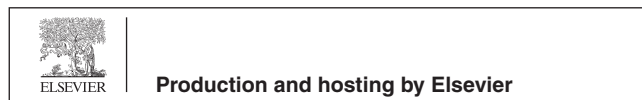
Intrusion detection in secure areas is a common application of motion detection. A very important application of motion detection is to limit video recording storage requirements to times of important events by starting the recording only at the start of an important event. This on demand recording helps avoiding continuous video recording of static scenes and speeds up video event analysis. Motion detection helps focusing on processing and storage of relevant events.

In this study, a new algorithm is presented which showed promising results compared with MSE (Winkler, 2005; Susstrunk and Winkler, 2004; Wang and Bovik, 2002) and Dynamic Template Matching DTM (Martinez-Martin and del Pobil, 2012a, b; Widyawan et al., 2012) based algorithms. The algorithm captures the video of a scene and detects motion by comparing successive frames in the video sequence based on

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the modeling of image luminance, contrast and structure at multiple scales.

The paper is organized as follows, in Section 2 some of the related work is presented; then, an overview of the basic and the proposed structural similarity index mechanisms for motion detection is presented. In Section 4, the performance of the proposed mechanism is evaluated using a set of experiments on both offline and online videos. Then, in Section 5, the efficiency of the proposed mechanism is proved by comparing it with the well-known GMM method of motion detection both analytically, by analyzing their memory requirements complexity and execution complexity, and experimentally by comparing their efficiency through a set of performance metrics.

## 2. Related work

Motion detection starts from a given frame as a reference and subsequent frame is compared with it; then the subsequent frame becomes a reference frame and the process is repeated with next frames. Mishra et al. (2011) discussed three commonly used methods to detect a motion: background subtraction, optical flow and temporal differences. Background subtraction was used by Spagnolo et al. (2006), Tang and Miao (2008), Li and Cao (2010) and it depends on a comparison of an image with a static reference image. The optical flow method specifies how much each pixel of the image moves between adjacent frames, this method may require additional hardware to support the performance and monitoring of systems (Allili et al., 2002; Jung et al., 2007). The temporal difference method relies on comparing consecutive frames by analyzing all frame pixels (Yu and Chen, 2009), e.g. by applying the concept of Sum of Absolute Difference (SAD), where SAD is used to determine whether there is a movement within an image pair (Kenchannavar et al., 2010).

There is a lot of research work based on the above methods and combinations of them. Kenchannavar et al. (2010) described an algorithm combining background subtraction and frame differences for motion detection. Zheng et al. (2009), Murali and Girisha (2009), Fang et al. (2009), used frame differences coupled with an adaptive threshold setting and statistical correlation to analyze the temporal differences in some of the image frames.

Other methods for motion detection exist in the literature. For example, Yong et al. (2011) studied four methods for motion detection: frame differences, background subtraction, pixelate filter, and blob counter. Li and Cao (2010) used Support Vector Machines (SVM) for motion detection and segmentation of moving objects. Yokoyama et al. (2009) applied the concept of vectors to movement detection by comparing multiple frames and marking the points of difference among the frames. An advantage of this method is that it yields information about the direction of object movement. Kameda and Minoh (1996) used the double difference technique for motion detection. Double differences are conducted by comparing two successive frames at times  $t$  and  $t - 1$  and then performing a second comparison between the frames at times  $t - 1$  and  $t - 2$ . In contrast, Collins and et al. (2000) reported a video surveillance and monitoring system which depends on comparisons between the image  $t$  with the image of  $t - 1$ , and the image  $t$  with the image of  $t - 2$ .

From the above, we can see that there are many research works done on the motion detection which uses different methods and have achieved different results.

## 3. Structural similarity index mechanisms for motion detection

The SSI measurement system (Wang and Bovik, 2002) is based on modeling of image luminance, contrast and structure. The MS-SSIM is an extension of the SSI system that achieves better accuracy than the single scale SSI approach but at the cost of relatively lower processing speed. However, the computations required for the MS-SSIM does not require such large computational time required by other efficient Statistical Learning Algorithms (Avcibas et al., 2002) since it requires complex calculations. Our system applies the MS-SSIM for motion detection in videos; either on online videos directly captured from camera, or on recorded video stored in a file. Any video is sequenced into frames and successive frames are compared with each other and if a difference is detected, an alarm is released.

The proposed approach relies on a new algorithm which helps local adaptation of the multi-scale structural similarity measure for motion detection in videos. In the next sections we present the basic SSI measurement system as it is the base of the used algorithm, the MS-SSIM; next we present MS-SSIM itself. Then, we present our proposed algorithm for motion detection using the MS-SSIM.

### 3.1. SSI measurement systems

The Structural Similarity Index (SSI) measurement, shown in Fig. 1, is based on modeling image luminance, contrast and structure.

Mathematically, the SSI is defined by Wang and Bovik (2006) as:

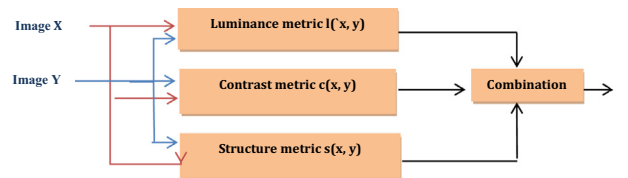
$$SSI(x, y) = \frac{(2\mu_x\mu_y + C_1)(2\sigma_{xy} + C_2)}{(\mu_x^2 + \mu_y^2 + C_1)(\sigma_x^2 + \sigma_y^2 + C_2)} \quad (1)$$

where  $\mu_x$ ,  $\mu_y$ ,  $\sigma_x$  and  $\sigma_y$  are the means and standard deviations of both the original and reference images respectively,  $C_1$  and  $C_2$  are constants. The three models considered in building the similarity index between the two images  $x$  and  $y$  are given by Lavielle (1999), Wang et al. (2003), and Wang et al. (2004):

$$\text{Luminance : } L(x, y) = \frac{2\mu_x\mu_y + C_1}{\mu_x^2 + \mu_y^2 + C_1} \quad (2)$$

$$\text{Contrast : } C(x, y) = \frac{2\sigma_x\sigma_y + C_2}{\sigma_x^2 + \sigma_y^2 + C_2} \quad (3)$$

$$\text{Structure : } S(x, y) = \frac{\sigma_{xy} + C_3}{\sigma_x\sigma_y + C_3} \quad (4)$$



**Figure 1** Structure similarity measurement system (Tolba and Raafat, 2015).

where  $\mu_x$ ,  $\sigma_x^2$  and  $\sigma_{xy}$  are the mean of  $x$ , the variance of  $x$ , and the covariance of  $x$  and  $y$  respectively, while  $C_1$ ,  $C_2$  and  $C_3$  are constants given by  $C_1 = (K_1L)^2$ ,  $C_2 = (K_2L)^2$  and  $C_3 = C_2/2$ .  $L$  is the dynamic range for the sample date, where,  $L = 255$  for 8 bit gray-level image and  $K_1 \ll 1$  and  $K_2 \gg 1$  are two scalar constants (Winkler, 2005; Susstrunk and Winkler, 2004). Given the above measures the structural similarity index of two images  $x$  and  $y$  can be computed as (Winkler, 2005; Susstrunk and Winkler, 2004; Lavielle, 1999; Wang et al., 2003, 2004):

$$ssi(x, y) = [l(x, y)]^\alpha [c(x, y)]^\beta [s(x, y)]^\gamma \quad (5)$$

where  $\alpha$ ,  $\beta$ ,  $\gamma$  define the weight given to each model. Fig. 2 shows the architecture of a motion detection system that is based on the SSI.

### 3.2. MS-SSIM measurement systems

The Multi Scale Structural Similarity Index for Motion Detection (MS-SSIM) quality metric is an extension of the SSI which computes these measures at various scales and combines them using an equation of the form (Lavielle, 1999; Wang et al., 2003, 2004):

$$MS - SSIM(x, y) = [l_m(x, y)]^{2M} \cdot \prod_{j=1}^M [C_j(x, y)]^{\beta_j} \cdot [S_j(x, y)]^{\gamma_j} \quad (6)$$

where,  $M$  corresponds to the lowest resolution (i.e. the times of down samplings performed to reduce the image resolution), while  $j = 1$  corresponds to the original resolution of the image. The resolution of the analyzed image has a significant impact on motion detection results. The interaction between motion size and image resolution also is an important factor. Therefore, using the MS-SSIM metric renders itself a good adaptive measure for motion detection. Fig. 3 presents the architecture of a novel system for Motion detection based on the multi-scale structural similarity index.

### 3.3. Proposed MS-SSIM based motion detection algorithm

The main steps of the proposed algorithm to detect motion in a video sequence using the MS-SSI, are shown in Fig. 4 and are summarized as follows:

- 1- The algorithm starts by loading the video file in case of a recorded video, or initializing video capturing through the camera in case of real time motion detection.
- 2- Then, the following steps are applied repeatedly on the successive frames of the captured video starting from time  $t = 0$ , i.e. first captured/loaded frame; until, in case of a recorded video, all video frames have been processed; or, in case of real time video, the camera stops capturing the scene:

- a. Capture/load one frame  $f_t$  at the time instant  $t$ .
- b. Capture/load the next frame  $f_{t+1}$  at time instant  $t + 1$ .
- c. Convert the two frames to gray level format.
- d. Compute the MS-SSIM ( $f_t, f_{t+1}$ ) index of the two successive frames.
- e. If the similarity between the two successive frames lies below a predetermined threshold  $\theta$  a motion activity is detected and an alarm is released.

In the above algorithm, the estimation of the appropriate threshold level for the MS-SSIM test is very critical to the success of the presented detection system.

## 4. Performance evaluation

In the following subsections, we present the results of applying the proposed algorithm in different cases on different video samples.

### 4.1. Test results of recorded video with predetermined number of motions

In the following test, the performance of the developed algorithm is evaluated using recorded videos. The changes between frames have been identified to detect the occurrence of a motion. To measure the performance for the proposed motion detection approach, we have adapted some performance measures discussed by Altman and Bland (1994), Lu and et al. (2004), Eisner and et al. (2005), and Sokolova et al. (2006), González et al. (2007). These measures are defined in our work as:

**True Still Stand (TSS):** Number of two successive frames where no motion is detected based on the agreement of both the system result and the ground truth.

**False Still Stand (FSS):** Number of two successive frames where no motion is detected while there is disagreement between the system result and the ground truth.

**True Motion Detection (TMD):** Number of two successive frames where motion is detected based on the agreement of both the system result and the ground truth.

**False Motion Detection (FMD):** Number of two successive Frames where motion is detected while there is disagreement between the system result and the ground truth.

**F-Score:** A measurement of the accuracy that considers both precision and sensitivity of the test to compute the score.

**Matthews' Correlation Coefficient (MCC):** A balanced measurement of the quality of binary classifications i.e. it is a correlation coefficient between the observed and the predicted binary classifications, where positive 1 value indicates perfect prediction, 0 indicates random average prediction and  $-1$  value indicates inverse prediction.

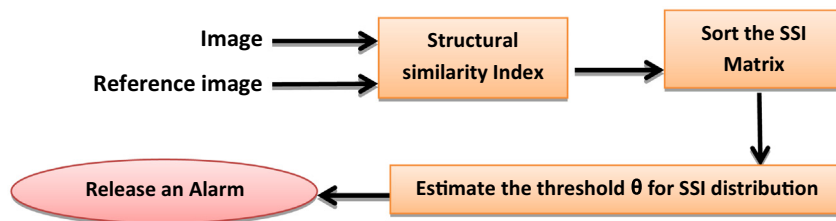


Figure 2 Architecture of the SSI based motion detection system [adapted from (Tolba and Raafat, 2015)].

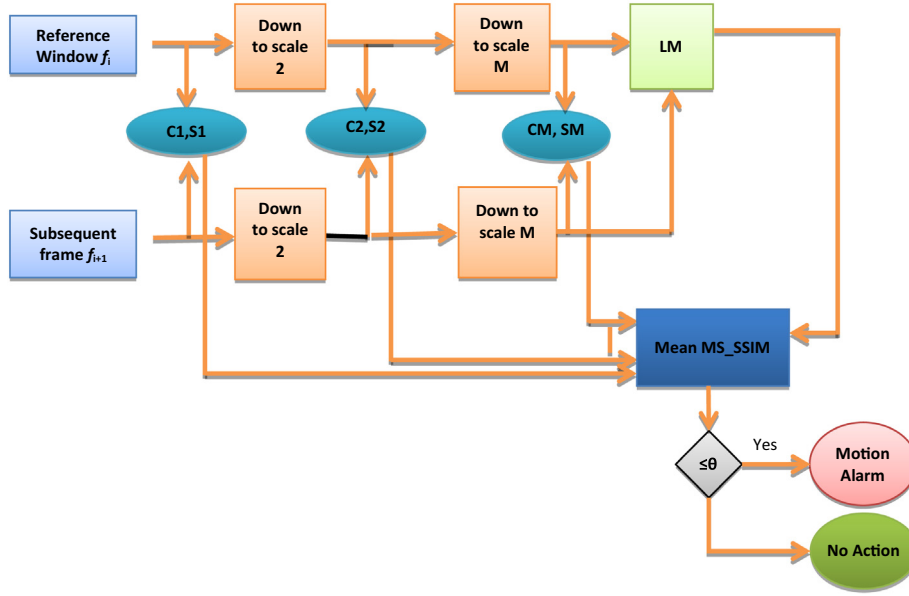


Figure 3 Architecture of the MS-SSIM based motion detection system.

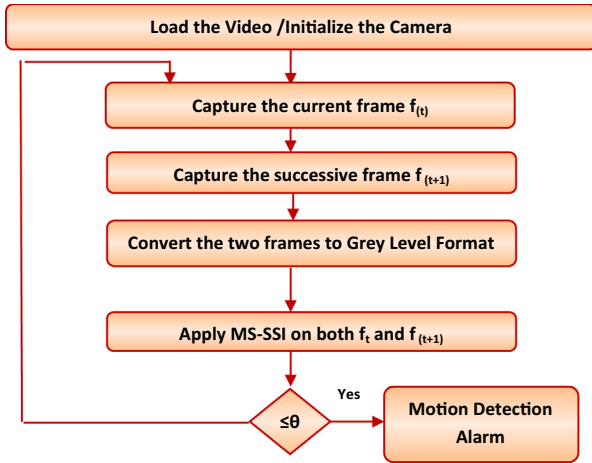


Figure 4 MS-SSIM based motion detection system.

From these measures, we used the following performance indicators of the motion detection system:

$$precision = \frac{TMD}{TMD + FMD} \quad (7)$$

$$Sensitivity = \frac{TMD}{TMD + FSS} \quad (8)$$

$$Specificity = \frac{TSS}{TSS + FMD} \quad (9)$$

$$Accuracy = \frac{TMD + TSS}{TMD + TSS + FMD + FSS} \quad (10)$$

$$Positive Prediction = \frac{TMD}{TMD + FMD} \quad (11)$$

$$Negative Prediction = \frac{TSS}{TSS + FSS} \quad (12)$$

$$False Negative Rate = \frac{FSS}{FSS + TMD} \quad (13)$$

$$False Positive Rate = \frac{FMD}{FMD + TSS} \quad (14)$$

$$F-score = \frac{(2 \times Precision \times Sensitivity)}{(Precision + Sensitivity)} \quad (15)$$

$$MCC = \frac{(TMD * FMD) - (TSS * FSS)}{\sqrt{((TMD + FSS) * (TMD + TSS) * (FSS + TMD) * (FSS + FMD))}} \quad (16)$$

Furthermore, we checked the quality of the proposed algorithm at different threshold values to measure the effect of the chosen threshold on the correctness of the algorithm.

In the experiments, we used three videos with pre-determined motion actions (ground truth), where each of these videos shows a clock with pointer(s) moving at a constant rate. The choice of such videos simplifies the visual detection of the motion occurrence and limits it to pre-determined values that can be easily compared with the motion detected by the proposed algorithm to measure the accuracy and efficiency of the proposed algorithm at different threshold values. The snapshot of the first video shown in Fig. 5, has a clock with a single *second pointer*, i.e. moving at a rate of 60 movements/minute. The video specifications are,

Length of video: 60 s. Number of frames: 615 frames.  
Frame size: 640 \* 360 size: 44.9 MB (Uncompressed).  
Frame rate 10 f/s.

From the above details, we can easily conclude that the video has 60 movements. By applying the proposed algorithm on this video at different threshold values we obtained the results shown in Table 1. From the results shown in the table,



an estimated number of the number of frames that has a motion. Then, at different values of the threshold and frame rate, we compare the actual number of frames detected by the proposed system;  $ndf$ , to the numbers of estimated frames ( $nef$ ). Also, another number of frames;  $nof$ , is counted by observing the same video and this value is compared as well to the values detected by the MS-SSI at different threshold and frame rate values.

Fig. 7 shows snapshots of a video captured in a restaurant using a static camera to monitor persons in the restaurant. The experiment is performed on a test video taken from the Image Sequence Evaluation (ISE) Lab (González et al., 2007), see a sequence of it in Fig. 7. The original video specifications are as follows:

- Duration of video: 00:02:13
- Number of frames: 3321 frames.
- Frame size: 1392 px, Height 1040 px,
- File format: AVI.
- Frame rate: 25 fps.

To get the frames' ROI in this video, it is found that there was no motion in the first 24 s; then, the persons started to appear and move in the scene from the moment at 00:24:00 up to the moment 01:36:00. In addition to that, there was a short moment of motion in other part of the video for less than one second. So, a total of around 73.5 s was assumed as the length of the ROI of the frames. This value was used to get the estimated number of frames in the ROI at three different frame rate values, 25, 18, 10 f/s, as shown in Table 5. The same table also shows the counted number of frames,  $nof$ .

Table 6 shows the number of the detected frames ( $ndf$ ) detected by the proposed MS-SSI approach at several values of the threshold obtained manually by observing the video.

**Table 3** Measurements of the detected frames in the second video.

	$\Theta$							
	0.96	0.965	0.97	0.975	0.98	0.985	0.99	0.995
TMD	0	0	5	33	47	57	60	61
TSS	544	544	544	544	544	544	544	544
FMD	0	0	0	0	0	0	0	0
FSS	61	61	56	28	14	4	1	0

The results of the two Tables 5 and 6 are used to draw the charts shown in Fig. 8 in order to analyze the efficiency of the MS-SSI with the change of the threshold value used in the algorithm and the frame rate of the analyzed video.

Fig. 8(a) shows clearly that the detection rate increases with the increase in the value of the threshold as expected from the previous experiments. Fig. 8(b) shows an interesting anomaly, where the detected number of frames, at any value of the threshold, for the 18 f/s is more than the detection rate of the 10 f/s but it is less than the 25 f/s. This is due to the fact that increasing the frame rate from 10 f/s to 18 f/s results in an increase in the number of frames of the video; and hence the number of frames in the frames of the period of the motion, which makes the MS-SSI able to detect higher number of frames. However, continuous increase in the value of the frame rate makes the differences between each two consecutive frames less noticeable by the algorithm and requires the use of a higher threshold value of the algorithm to be detected; hence, resulting in a decrease in the number of the detected frames of motion. Fig. 8(c and f) gives a better comparison by avoiding variation of the numbers of frames in the three versions of the video, by normalizing the number of detected frames to the number of estimated and observed frames, i.e.  $ndf/nef$  and  $ndf/nof$  respectively in the period of interest.

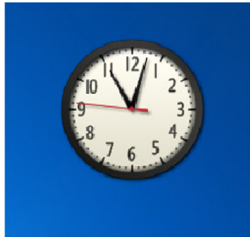
Fig. 8(c) shows clearly that the detection efficiency increases with the increase in the threshold, where the detection reaches high values for 10 f/s than the cases of 18 f/s and 25 f/s, i.e. increasing the frame rate requires the use of higher threshold values to get higher detection efficiency. The same Figure shows that a threshold value of 0.99 results in the detection of a ratio around 100% for the 10 f/s, but using this value in case of the 18 f/s results in 69% and only 50% in case of 25 f/s. Fig. 8(d), shows this clearly, as the chart lines are monotonically decreasing with a sharp slope, i.e. the increase in the frame rate results in lower detection efficiency of the MS-SSI. The low detection ratios of Fig. 8(c and d) may indicate inefficiency of the proposed MS-SSI at high frame rates, but looking at Fig. 8(e) gives a better indication as it shows the ratio of the detected motion by the MS-SSI to the number of motion frames *observed* by humans, which is more sensible.

Fig. 8(e) shows that the MS-SSI resulting motion detection for both 10 f/s and 18 f/s are very close to each other for all values of the threshold, while for the 25 f/s it was a bit less for low threshold values until the threshold value of 0.985, where its starts to be very close to the 10 f/s and the 18 f/s and at a threshold value of 0.99 it has made a 0.98% detection success. This is again due to the fact that using high frame rate

**Table 4** Performance metrics obtained by applying MS-SSIM on the second video at different threshold values.

$\Theta$	Sensitivity	Specificity	Accuracy	Precision	Positive prediction	Negative prediction	False negative rate	False positive rate
0.960	0.016	0.901	0.899	0.333	–	0.899	1.00	0.000
0.965	0.016	0.901	0.900	0.333	–	0.899	1.00	0.000
0.970	0.483	0.946	0.946	0.935	1.00	0.907	0.918	0.000
0.975	0.750	0.996	0.972	0.957	1.00	0.951	0.460	0.000
0.980	1.000	0.996	0.997	0.970	1.00	0.975	0.230	0.000
0.985	1.000	0.996	0.996	0.970	1.00	0.993	0.066	0.000
0.990	1.000	0.995	0.995	0.952	1.00	0.998	0.016	0.000
0.995	1.000	0.968	0.970	0.770	1.00	1.000	0.000	0.000
Average	0.917	99.61	0.988	0.966	1.000	0.973	0.450	0.000

[0.975:0.985]



**Figure 6** Snapshot of the second video with known number of motions.

results in consecutive frames with very similar structure that requires high threshold values to be detected by the MS-SSI. The same result is deduced from Fig. 8(f); at low threshold values, the chart lines decrease with the increase in the frame rate, while at high threshold values the lines look constant; i.e. the ratio  $ndf/nof$  is constant versus the frame rate change. From the above, it is seen that the value of the threshold should be taken between 0.985 and 0.995, with a recommendation of using values closer to 0.995 for the videos with a high frame rate.

#### 4.3. Results of motion detection in real time video

Real time videos captured using a webcam has been used to test the algorithm. The frames of the video sequence were captured at a resolution of  $192 \times 256$  and converted to gray level. The sequence included 1236 frames. The MS-SSIM algorithm has succeeded in motion detection with a true positive rate of

99.1% at a threshold value of 93%. The DTM algorithm resulted in only 89.9% correct detection rate. This clearly shows the efficiency of the proposed method relative to the classical methods of motion detection.

#### 5. Efficiency evaluation

As stated earlier, existing techniques for motion detection include methods based on optical flow, frame difference, template matching and background subtraction methods. Among those, Background subtraction methods have been proven to be the most efficient as indicated by Sun and et al. (2004), Xie, 2013, and Benzeth et al. (2010). Hence, in this section, we evaluate the efficiency of our proposed MS-SSI based motion detection algorithm by comparing it with one of the most efficient background subtraction methods (Benzeth et al., 2010); the Gaussian Mixture Model (GMM). The main idea of the GMM method is to use multimodal probability density functions, where every pixel within a frame is modeled with a mixture of  $K$  Gaussians; hence, the probability of occurrence of a color  $p(I_{s,t})$  at a given pixel  $s$  in frame  $t$  is given by:

$$p(I_{s,t}) = \sum_{i=1}^K w_{i,s,t} N\left(\mu_{i,s,t}, \sum_{i,s,t}\right) \quad (17)$$

where  $N(\mu_{i,s,t}, \sum_{i,s,t})$  is the  $i$ th Gaussian model,  $w_{i,s,t}$  is its weight,  $\mu_{i,s,t}$  is the  $i$ th Gaussian mean and  $\sum_{i,s,t}$  is the covariance matrix. The weight  $w_{i,s,t}$  of each distribution is updated for each frame according to the equations in Benzeth et al. (2010).



**Figure 7** Snapshot of the video with continuous motion.

**Table 5** Average system performance indicators for MS-SSIM when applied on the video shown in Fig. 7.

	Observed movements at frame rate		
	10 f/s	18 f/s	25 f/s
Total number of frames in the video	1331 frames	2394 frames	3321 frame
Estimated frames in the ROI ( <i>nef</i> )	738 frames	1324 frame	1833 frame
Observed frames of motion ( <i>nof</i> )	738 frames	888 frames	918 frames

**Table 6** Measurements of the detected frames in the video shown in Fig. 7.

Threshold value	Total detected frames ( <i>ndf</i> ) of movements at		
	10 f/s	18 f/s	25 f/s
0.930	348	382	316
0.940	381	433	360
0.950	434	502	404
0.960	510	572	474
0.965	510	572	474
0.970	571	655	581
0.975	571	655	581
0.980	626	763	715
0.985	626	763	715
0.990	760	910	908
0.995	760	910	908

In the following, we compare the proposed method with the GMM method in three main aspects: the memory requirements, computation time complexity and the accuracy.

### 5.1. Memory requirements analysis

For the basic GMM model, the memory storage space required is  $5K$  floats per pixel (Benezeth et al., 2010), where  $K$  is the number of distributions built per pixel and  $K$  is practically taken between 3 and 5, this relatively big storage area is due to the need for representing every pixel with  $K$  probability density function. On the contrary, our proposed method, which is based on the MS-SSIM, computes at various scales from 1 down to  $M$ , the contrast and the structure terms; in addition to the luminance at the lowest scale only. Hence, the main storage  $S_{frame}$  required for storing and processing the pixels in a single video frame processed using this method can be calculated by summing up the sizes required for processing all the pixels in this frame at all the scales from 1 to  $M$  as follows:

$$S_{frame} = N_{pixels[1...M]} \cdot S_{cs-pixel} + N_{(M)} \cdot S_I \quad (18)$$

where,  $N_{pixels[1...M]}$  is the total number of pixels processed at all scales from 1 to  $M$ ,  $S_{cs-pixel}$  is the storage size required for processing one pixel to get both its structure and contrast values at a certain scale,  $N_M$  is the number of pixels at scale  $M$  and  $S_I$  is the storage required for luminance.

$N_{pixels[1...M]}$  can be calculated as follows:

$$N_{pixels[1...M]} = S_{ScaleF(1)} + S_{ScaleF(2)} + \dots + S_{ScaleF(M)} \quad (19)$$

where  $S_{ScaleF(i)}$  is the number of pixels in frame  $i$ ; hence,

$$N_{pixels[1...M]} = (1 + (1/(2.2)) + \dots + (1/(M.M))). S_{ScaleF(1)}$$

It is easily to conclude that,

$$N_{pixels[1...M]} < 2 \cdot S_{ScaleF(1)}, \quad (20)$$

where  $S_{ScaleF(1)}$  is frame size at scale 1. Hence, from the above and as  $N_M = S_{ScaleF(M)} < S_{ScaleF(1)}$

$$S_{frame} < 2 \cdot S_{ScaleF(1)} \cdot S_{cs-pixel} + S_{ScaleF(1)} \cdot S_I \quad (21)$$

Hence, we can conclude that the storage required to calculate the MS-SSI of a single pixel  $S_{MS-SSI-pixel}$  can be given by  $S_{MS-SSI-pixel} < (2 \cdot S_{ScaleF(1)} \cdot S_{cs-pixel} + S_{ScaleF(1)} \cdot S_I) / S_{ScaleF(1)}$ ; hence,

$$S_{MS-SSI-pixel} < 2 \cdot S_{cs-pixel} + S_I \quad (22)$$

In MS-SSI, to calculate both  $S_{cs-pixel}$  and  $S_I$  for each pixel, a  $11 \times 11$  window is typically used at each pixel, to get both the contrast and the structure values as indicated in equations (Susstrunk and Winkler, 2004; Wang and Bovik, 2002; Martinez-Martin and del Pobil, 2012a, b) then the same window moves to the next pixel. Hence, only 2 floats are required to save both the structure and the contrast at each pixel, i.e.  $S_{cs-pixel} = 2$ , and only one float is required for the luminance value, i.e.  $S_I = 1$ . Hence, by substituting in the above equation,  $S_{MS-SSI-pixel} < 5$ , i.e. the proposed method which is based on the MS-SSIM requires less than 5 floating point operations for processing each pixel in a video frame, which is  $K$  times less storage than the GMM-based method.

### 5.2. Time complexity analysis

For the computation time, the GMM is much more complicated and consumes more time as it involves several stages including:

- Calculate  $K$  Gaussian distributions for each pixel in each frame.
- Update the weights of the distributions from a frame to another.
- Order the distributions and extract the best background model for each frame.
- Segment the foreground and detect the motion by subtracting it from the foreground of the previous frame.

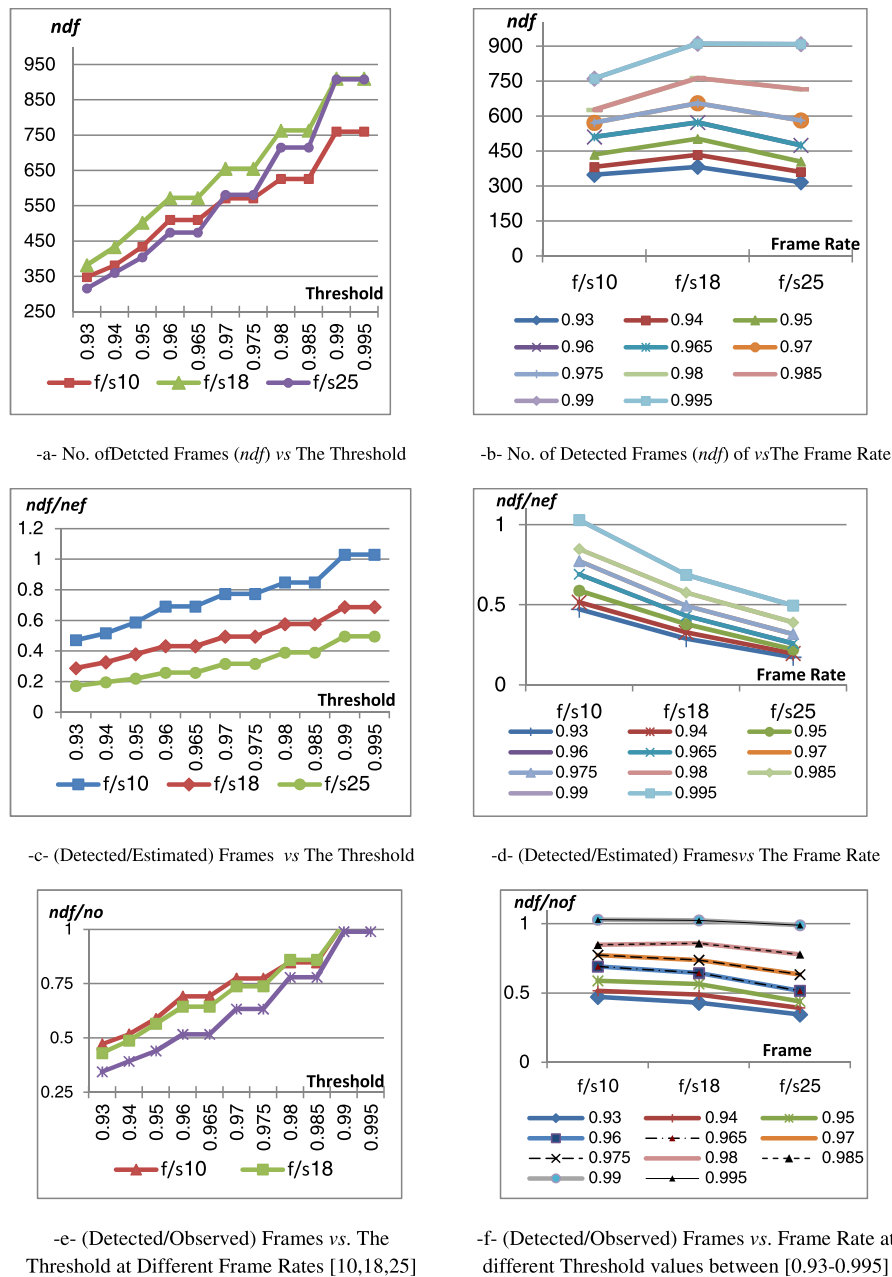
All these operations make GMM much more time consuming when compared to the proposed MS-SSIM. MS-SSIM requires processing a number of pixels  $N_{pixels[1...M]} < 2 \cdot S_{ScaleF(1)}$ , where it requires for each pixel only one distribution to use it with the distribution of the pixel at the same location in the following frame to calculate both the structure and the contrast; then, the luminance is calculated only once on the last scaled down image. Hence; the time complexity to process the pixels in one video frame using our MS-SSIM based method is given by:

$$T_{single-frame} = N_{pixels[1...M]} \cdot T_{sc} + N_M \cdot T_I \quad (23)$$

However, Both  $T_{sc}$  and  $T_I$  are constants as they use a fixed  $11 \times 11$  window. Hence,

$$T_{single-frame} = c_1 \cdot N_{pixels[1...M]} + c_2 \cdot N_M = O(N_{pixels[1...M]}) \text{ as } N_M \text{ is much less than } N_{pixels[1...M]}$$





**Figure 8** Effect of threshold and the frame rate on the MS-SSSI.

As  $N_{pixels[1...M]} < 2 \cdot S_{ScaleF(1)}$ , hence, the MS-SSIM requires a number of iterations less than twice the video frame size to detect the motion. In contrast to GMM, to run the first stage, i.e. to get the  $K$  distributions of each pixel requires a number of times equals  $K$  times the frame size. This means the whole processing of the proposed MS-SSIM is faster than the first stage of the GMM-based method, which clearly emphasizes the efficiency of the proposed method.

### 5.3. Performance of detection

To compare their performance, both the GMM method and the proposed method have been tested on the videos shown earlier in Figs. 5–7. Table 7 explores the average performance

**Table 7** Comparison between GMM and the proposed method.

Performance Indicators	MSSI-MD	GMM
Sensitivity	92%	93%
Specificity	100%	99.8%
Accuracy	99.2%	99.1%
Precision	100%	98.3%
F-score	0.9583	0.9558
MCC	0.17	-0.09
Positive-prediction	91.5%	98.3%
Negative-prediction	100%	99.6%
False-negative-rate	0	3.3%
False-positive-rate	1.1%	0.18%

measurements of both methods on both videos. It is clear that the proposed method provides very high specificity, accuracy and precision in the detection with very high sensitivity, F-Score, a positive MCC and very low false rates in comparison with the GMM.

## 6. Conclusions

This work presents an efficient novel approach for detection of motion occurrence within videos. It measures the similarity of successive frames of a video using the Multi Scale Structural Similarity Index. The proposed approach has achieved very high motion detection accuracy in most of the conducted experiments; its efficiency depends on the used threshold, where it gives the best results for values between 0.985 and 0.995 in most experiments. The experimental results show that the proposed MS-SSIM-based method has resulted in better performance than the single scale SSI approach but at the cost of relatively lower processing speed, this reduction in speed is expected as it applies the SSI on several scales. In comparison, with existing high efficient methods, the proposed method has shown to provide high efficiency with high speed and relatively low storage requirements which make it a great candidate for use in embedded devices with limited resources. The major advantages of the presented approach are: the higher detection accuracy and the quasi real-time processing speed. The resilience of the proposed approach to luminance, contrast and structural changes makes it very suitable for motion detection applications. The proposed approach at the moment detects the motion occurrence not the moving objects; in the future, we plan to integrate it with other existing approaches for detecting the moving objects. Also, further research will focus on the area of integrating the developed MS-SSIM into embedded systems with other non-camera based motion detection approaches to build multi-sensing modalities for motion detection.

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